Please check the examination deta	ails below	before entering yo	ur candidate information
Candidate surname		Other	names
Pearson Edexcel Level 3 GCE	Centre	e Number	Candidate Number
Tuesday 23 Ju	une	2020	
Afternoon (Time: 1 hour 30 minutes) Paper Reference 9FM0/4A			
Further Mather Advanced Paper 4A: Further Pure			
You must have: Mathematical Formulae and Stat	tistical T	ahles (Green)	Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B)
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for each question are shown in brackets
 use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶







1.	A small sports club has 12 adult members and 14 junior members.	
	The club needs to enter a team of 8 players for a particular competition.	
	Determine the number of ways in which the team can be selected if	
	(i) there are no restrictions on the team,	(1)
		(1)
	(ii) the team must contain 4 adults and 4 juniors,	(2)
	(iii) more than half the team must be adults.	
		(3)

Question 1 continued	
/T	otal for Question 1 is 6 marks)
(1	our for Arcenon 1 is a marks)



2. Solve the recurrence system		
	$u_1 = 1 u_2 = 4$ $9u_{n+2} - 12u_{n+1} + 4u_n = 3n$	
	n_{n+2} n_{n+1} n_n n_n	(9)

4

Question 2 continued



Question 2 continued

Question 2 continued	
(Total	for Question 2 is 9 marks)
(10tal	ZOZ ZOROWANIA ZO Z ARREATED)



3.

$$\mathbf{M} = \begin{pmatrix} 1 & k & -2 \\ 2 & -4 & 1 \\ 1 & 2 & 3 \end{pmatrix}$$

where k is a constant.

(a) Show that, in terms of k, a characteristic equation for M is given by

$$\lambda^3 - (2k+13)\lambda + 5(k+6) = 0$$
(3)

Given that $\det \mathbf{M} = 5$

- (b) (i) find the value of k
 - (ii) use the Cayley-Hamilton theorem to find the inverse of M.

(7)

Question 3 continued



Question 3 continued

Question 3 continued
(Total for Question 3 is 10 marks)



4.

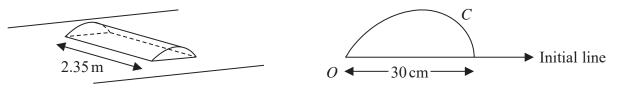


Figure 1

Figure 2

Figure 1 shows a sketch of a design for a road speed bump of width 2.35 metres. The speed bump has a uniform cross-section with vertical ends and its length is 30 cm. A side profile of the speed bump is shown in Figure 2.

The curve C shown in Figure 2 is modelled by the polar equation

$$r = 30(1 - \theta^2) \qquad 0 \leqslant \theta \leqslant 1$$

The units for r are centimetres and the initial line lies along the road surface, which is assumed to be horizontal.

Once the speed bump has been fixed to the road, the visible surfaces of the speed bump are to be painted.

Determine, in cm², the area that is to be painted, according to the model.

(10)

Question 4 continued



Question 4 continued

Question 4 continued	
	(Total for Question 4 is 10 marks)
	· · · · · · · · · · · · · · · · · · ·



5. A transformation T from the z-plane to the w-plane is given by

$$w = \frac{1 - 3z}{z + 2i} \qquad z \neq -2i$$

The circle with equation |z + i| = 3 is mapped by *T* onto the circle *C*.

(a) Show that the equation for C can be written as

$$3|w+3| = |1+(3-w)i|$$
 (4)

- (b) Hence find
 - (i) a Cartesian equation for C,
 - (ii) the centre and radius of *C*.

(6)

Question 5 continued	



Question 5 continued

Question 5 continued	
	Total for Question 5 is 10 marks)



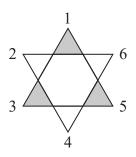


Figure 3

Figure 3 shows a plane shape made up of a regular hexagon with an equilateral triangle joined to each edge and with alternate equilateral triangles shaded.

The symmetries of this shape are the rotations and reflections of the plane that preserve the shape and its shading.

The symmetries of the shape can be represented by permutations of the six vertices labelled 1 to 6 in Figure 3. The set of these permutations with the operation of composition form a group, G.

(a) Describe geometrically the symmetry of the shape represented by the permutation

$$\begin{pmatrix}
1 & 2 & 3 & 4 & 5 & 6 \\
3 & 4 & 5 & 6 & 1 & 2
\end{pmatrix}$$

(2)

(b) Write down, in similar two-line notation, the remaining elements of the group G.

(4)

- (c) Explain why each of the following statements is false, making your reasoning clear.
 - (i) G has a subgroup of order 4
 - (ii) G is cyclic.

(2)

Diagram 1, on page 23, shows an unshaded shape with the same outline as the shape in Figure 3.

(d) Shade the shape in Diagram 1 in such a way that the group of symmetries of the resulting shaded shape is isomorphic to the cyclic group of order 6

(2)



Question 6 continued	



Question 6 continued

Question 6 continued
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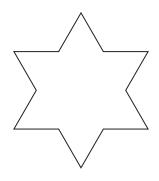
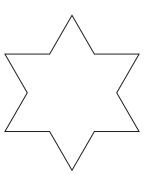


Diagram 1

Spare copy of Diagram 1



Only use this diagram if you need to redraw your answer to part (d).

(Total for Question 6 is 10 marks)



7. $I_n = \int (4 - 1)^n (4 - 1)^n dt$

$$I_n = \int (4 - x^2)^{-n} \, \mathrm{d}x \qquad n > 0$$

(a) Show that, for n > 0

$$I_{n+1} = \frac{x}{8n(4-x^2)^n} + \frac{2n-1}{8n}I_n$$

(5)

(b) Find I_2

(3)

Question 7 continued	



Question 7 continued

Question 7 continued	
Т	Total for Question 7 is 8 marks)
(1	ZVI VICELIOI / ID O HIGH IND)



- **8.** The four digit number n = abcd satisfies the following properties:
 - (1) $n \equiv 3 \pmod{7}$
 - (2) n is divisible by 9
 - (3) the first two digits have the same sum as the last two digits
 - (4) the digit b is smaller than any other digit
 - (5) the digit c is even
 - (a) Use property (1) to explain why $6a + 2b + 3c + d \equiv 3 \pmod{7}$

(2)

(b) Use properties (2), (3) and (4) to show that a + b = 9

(4)

(c) Deduce that $c \equiv 5(a-1) \pmod{7}$

(2)

(d) Hence determine the number n, verifying that it is unique. You must make your reasoning clear.

(4)



Question 8 continued	



Question 8 continued	



Question 8 continued	
	(Total for Question 8 is 12 marks)
	TOTAL FOR PAPER IS 75 MARKS

